# A study of vaporization enthalpy of pure hydrocarbons 

O. Rebas ${ }^{1 *}$, H. Zait ${ }^{1}$, N. Skander ${ }^{2}$ and E. C. Chitour ${ }^{1}$<br>${ }^{1}$ Laboratory of Valorization of Fossil Energies, Department of Chemical Engineering, Polytechnic National School, Algiers, Algeria.<br>${ }^{2}$ Sonatrach, Djenane El-Malik, Hydra, Algiers, Algeria.


#### Abstract

In this research, we employed a new method to calculate vaporization enthalpy of pure hydrocarbons. This equation is a function of the temperature, far from critical point and was tested for simple mixtures and oil fractions. Comparing values with the literature, the equation established have improved results in term of average standard deviation. We also applied the equation to the oil fractions; it required a characterisation of these complex mixtures. Excellent results are obtained, which are comparable or better than those obtained with other models.


Key words: Hydrocarbons, simple mixtures, oil fractions, enthalpy of vaporization, group contribution, intramolecular interactions.

## INTRODUCTION

The method of group contribution has great success and remarkable development, considering the reliability of the results which they provide. However, their application beyond the field in which they were defined can involve significant errors. To mitigate the insufficiencies of the existing methods, we set up a new correlation of group contributions with interactions, which has a better prediction of the enthalpy of vaporization of pure hydrocarbons, mixtures and oil fractions according to the temperature.
Some of the group contribution methods for estimation of enthalpy of vaporization were devlopped. We cite some of them: Constantinou and Gani (1994) for predicting the enthalpy of vaporization Standard 298K; Svoboda and Dockalova (1990) have proposed a group contribution equation to estimate the heat of vaporization as a function of reduced temperature. An extension of this method to other types of compounds was performed by Basarova and Svoboda (1995) who propose using the

[^0]following expression in which the terms A and $\alpha$ are expressed in terms of group contribution:
\[

$$
\begin{equation*}
\Delta H v=A\left(1-T_{r}\right)^{\alpha} \exp (-\alpha T) \tag{1}
\end{equation*}
$$

\]

Li et al. (1997) proposed a method for estimating the enthalpy of vaporization at different temperatures by combining the principles of corresponding states and group contribution. In this method, two equations are established. The first is similar to the equation of Watson (1943) in which the term on the critical temperature is expressed as an equation group contribution. This equation requires knowledge of the enthalpy of vaporization at boiling point. The second equation is obtained by replacing the standard enthalpy of vaporization in the first equation by a relationship similar to the equation of Riedel (1954) which gives the enthalpy of vaporization at normal boiling temperature. The critical parameters that are used in this equation are evaluated for their contribution in terms of groups.

In addition to the Riedel's (1954) equation, other

Table 1. Chemical groups.

| Structural group | Characteristic |
| :--- | :--- |
| $-\mathrm{CH}_{3} \quad-\mathrm{CH}_{2}-$ | Normal paraffin |
| $-\mathrm{CH}<>\mathrm{C}<$ | Ramified paraffin |
| $=\mathrm{CH}=\mathrm{CH}-=\mathrm{C}<=\mathrm{C}=$ | Olefin |
| $\equiv \mathrm{CH} \equiv \mathrm{C}-$ | Alkyne compound |

correlations have been proposed in the literature to estimate the enthalpy of vaporization at normal boiling tempe-rature. Among them we cite the equations of Chen (1965) and Vetere (1973). The equations of Skander et al. (1999) based on the number of groups $-\mathrm{CH}_{2}$-for families of hydrocarbons is presented thus:

$$
\begin{equation*}
\Delta H_{v}=a+b /\left[1+\left(\left(N_{c}\right) / c\right)^{d}\right] \tag{2}
\end{equation*}
$$

$a, b, c$ and $d$ are constants whose values were determined in the case of n-paraffins, n-alkylcyclohexanes and n-alkylbenzenes. Meyra et al. (2004) suggested the following expression to calculate $\Delta H^{\text {vap }}$ :

$$
\begin{equation*}
\Delta H v a p=\left.\Delta H_{t}^{v a p}\right|_{\mid T_{c}-T_{t}} ^{T} \overbrace{c}^{T} z_{c}^{2}\left[\left(T_{c}-T\right) /\left(T_{c}-T_{t}\right)\right]+Z_{c} \tag{3}
\end{equation*}
$$

Where $T_{\mathrm{t}}$ is the temperature in the triple point and $Z_{\mathrm{c}}$ is the universal critical ratio. In the work of Meyra et al. (2004) the work of Guggenheim's (1945) theory was employed for determination of $Z_{\mathrm{C}}$, which was around
0.292. In Ricardo et al. (2005), three different theories (Reid et al., 1987) were used for determination of $Z_{\mathrm{C}}$. Three different values for $Z_{\mathrm{C}}\left(Z_{\mathrm{C} 1}\right.$ : Guggenheim theory (1945) $Z_{\mathrm{c} 2}$ : state correspondent theory; and $Z_{\mathrm{c} 3}$ : semiempirical value) were used in the Meyra's equation to check if it would have a marked effect in the results. The calculations have also been referenced at the normal boiling point.

The enthalpy of vaporization of simple mixtures can be determined by the rule of Kay (1936) for simple mixture expressed in molar percentages. For petroleum fractions, the method of additivity and correlations of Riazi and Daubert (1980, 1987), can be used. These last equations require knowledge of the mean-average temperature and specific-gravity of the fraction.

This article deals with the proposal of a methos predicting $\Delta \mathrm{Hv}$, using group contribution method with interactions. Then, we apply our correlation to the mixtures, quantitatively and qualitatively known. Finally, we tested the new equation to the oil fractions, using the conventional rules of additivity.

## PURE HYDROCARBONS

The steps followed for the development of the new method of group contribution with interactions is further described.

## Collection data

This stage consisted of the collection data of the enthalpy of vaporization of pure hydrocarbons belonging to various chemical families starting from the data banks developed by research centers (DIPPR, 1995). This operation made it possible to collect the values of the enthalpy of vaporization in function of the temperature, far from the critical point [100 to 650 K ] of hydrocarbons:
$\left.\Delta H_{v}=A \left\lvert\, 1_{( }^{\left(-\frac{T}{I_{c}}\right)}\right.\right)^{B}$
The general equation relating $\Delta \mathrm{Hv}$ ( $\mathrm{j} / \mathrm{kmole}$ ) at the tem-perature T (K) has been given from DIPPR database (DIPPR, 1995). It is defined thus: The parameters A, B are constants that could be assessed by the method of group contribution with interactions for various famillies.

## Definition of the structural groupings

From the established database, we preceded to the choice of the structural groups which is the most likely to contribute to the various macroscopic properties of the studied hydrocarbons. For each
families group of hydro-carbons, we have selected some chemical groups as presented in Table 1.

By choosing these groupings, we make the distinc-tion be-tween structural groups present in linear chains and in a cycle. For example, the contribution group $-\mathrm{CH}_{2}$ present in $n$-hexane is not the same as in cyclohexane.

## Definition of the principal terms of interactions between structural groups and their environments

The steps followed to introduce the terms of interactions into the correlation of group-contribution are as follows:
riting the semi formula developed for each hydrocarbons family,
efining the principal terms of interactions, the hydrocarbons are characterized by their chemical nature (for example, normal paraffin $\mathrm{C}_{5} \mathrm{H}_{12}$ ) and their groups:
i. by the structural groups $A-$ and -B - which are respectively $\mathrm{CH}_{3}-$ and $-\mathrm{CH}_{2}$-, whose assembly constitutes a carbonic chain A-B-B-B-A [ $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ ]
y the principal groups of interactions A-B-B- and -B-B-B-, they are interaction terms between structural groups and their environment.
3. C
lassifying, in decreasing order, the principal interac-tion groups number compared to the molecules number for each family.

Tables 2 and 3 give the various principal groupings of inter actions for each family of hydrocarbons. Example of principal terms of interactions between structural groupings and their environments is presented in Figures 1 to 4.

Table 2. Main groupings of interactions of the normals paraffins, isoparaffins and olefins.

| Principal grouping of interaction |  |  |
| :---: | :---: | :---: |
| n-paraffin | Isoparaffin | Olefin |
| $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{-}$ | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{2}-$ | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ |
| $\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{-}$ | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ |
| $\mathrm{CH}_{3} \ldots .-\mathrm{CH}_{3}$ | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{3}$ | $-\mathrm{CH}_{2}-\mathrm{CH} 2-\mathrm{CH}=$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2} \mathrm{CH}_{2}-$ | $-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}_{2}$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{2}-$ |
|  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}$ | $\mathrm{CH}_{3}-\mathrm{C}=\mathrm{CH}_{2}-$ |
|  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{2}-$ | - $\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}=$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}_{2}-$ | $-\mathrm{CH}_{2}-\mathrm{C}=\mathrm{CH}_{2}$ |
|  | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}-$ | $-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}-$ |
|  | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{C}-$ | $\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}-$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}-$ | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{3}$ |
|  | $\mathrm{CH}_{3} \mathrm{CH}-\mathrm{CH}-$ | $\mathrm{CH}_{3}-\mathrm{C}=\mathrm{CH}-$ |
|  | $\mathrm{CH}_{3} \mathrm{C}-\mathrm{CH}-$ |  |
|  | $-\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}_{2}-$ |  |
|  | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{C}-$ |  |
|  | $-\mathrm{CH}-\mathrm{CH}_{2}-\mathrm{C}-$ |  |
|  | -CH-CH-C- |  |

Figure 1. Isoparaffin «4,5 dimethylheptane».

Figure 2. Number of principal groupings of interactions.


## ESTABLISHMENT OF NEW CORRELATIONS OF GROUP CONTRIBUTION WITH INTERACTIONS

In our case, to establish our correlation, we test various mathematical equations stemming from the generalized form $F(\theta)$ relating the property $\theta$, $i$ and $j$ types contributions, as Equation (1) shows:
$F(\theta)=a+b \times\left(\sum n_{i} \Delta \theta_{i}+\sum_{m} n_{j} \Delta \theta_{j}\right)+c \times\left(\sum n_{i} \Delta \theta_{i}+\sum_{n} n_{j} \Delta \theta_{j}\right)^{m}+d \times\left(\sum n_{i} \Delta \theta_{i}+\sum_{\mathrm{CH}_{2}} n_{j} \Delta \theta\right)_{\mathrm{CH}}^{n}$
$\left.n_{j} \Delta \theta_{j}\right)+c \times\left(\sum n_{i} \Delta \theta_{i}+\sum n_{j} \Delta \theta_{j}{ }^{m}\right)+d \times\left(\sum n_{i} \Delta \theta_{i}+\sum n_{j} \Delta \theta_{j}\right)$
$F$ is a mathematical function which can take various forms as presented in Table 4. The parameters $a, b, c, d$, $\mathrm{m}, \mathrm{n}$ and p are constants that could be assessed by the multilinear regression using the Marquardt-Levenberg algorithm. The twenty equations make it possible to test various mathematical functions and then the equation which provides the weakest variation, compared to the data of the tables taken as reference, could be selected.

With the convergence of the iterative process, the values of the parameters of the various equations are determined and their performances are evaluated by means of the average absolute deviation (AAD) compared to the values of the data bank.

## Selection of new correlations

To select the best correlations among the twenty tested,


Figure 4. Number of principal groupings of interactions; a) cycles
b) ramifications; c) cycles-ramifications.

Table 3. Main groupings of interactions of naphtenes and aromatics.

| Principal grouping of interaction | Cycle | Ramification | Cycle-ramification |
| :---: | :---: | :---: | :---: |
| Naphtene | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ |  |  |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ |  |  |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}_{2}-$ |  | $\mathrm{CH}_{3}-\mathrm{CH}_{\mathrm{c}}-\mathrm{CH}_{\mathrm{c}}{ }^{-}$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}-$ |  | $-\mathrm{CH}_{2 r-} \mathrm{CH}_{2 r-} \mathrm{CH}_{c}-$ |
|  | $-\mathrm{CH}-\mathrm{CH}-\mathrm{CH}-$ |  | $\mathrm{CH}_{3 r-}-\mathrm{CH}_{2 r-}-\mathrm{CH}_{\mathrm{c}}{ }^{-}$ |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}-$ | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | $\mathrm{CH}_{3}-\mathrm{C}_{\mathrm{c}-}-\mathrm{CH}_{2 \mathrm{c}}-$ |
|  | $-\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}_{2}-$ | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | $\mathrm{CH}_{3 r-} \mathrm{Cc}_{\mathrm{c}-\mathrm{CH}}^{3 r-}$ |
|  | $-\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}-$ |  |  |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{C}-$ |  |  |
|  | $-\mathrm{CH}-\mathrm{CH}_{2}-\mathrm{CH}-$ |  |  |
|  | $-\mathrm{C}-\mathrm{CH}_{2}-\mathrm{CH}-$ |  |  |
|  | - $\mathrm{C}-\mathrm{CH}_{2}-\mathrm{C}-$ |  |  |
| Aromatic | $=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}-$ |  | $-\mathrm{CH}_{2 r}-\mathrm{C}-\mathrm{CH}=$ |
|  | $=\mathrm{CH}-\mathrm{CH}=\mathrm{C}-$ |  | $-\mathrm{CH}_{2 \mathrm{r}}-\mathrm{C}=\mathrm{CH}-$ |
|  | $-\mathrm{CH}=\mathrm{CH}-\mathrm{C}=$ | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | $-\mathrm{CH}_{2 r-}-\mathrm{CH}_{2 r}-\mathrm{C}=$ |
|  | $-\mathrm{CH}=\mathrm{C}-\mathrm{CH}=$ | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | $\mathrm{CH}_{3} \mathrm{-} \mathrm{C}=\mathrm{CH}-$ |
|  | $-\mathrm{C}=\mathrm{CH}-\mathrm{C}=$ |  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}=$ |
|  | - $\mathrm{C}=\mathrm{C}-\mathrm{CH}=$ |  | $\mathrm{CH}_{3 \mathrm{r}-\mathrm{CH}-\mathrm{C}=}$ |
|  | $=\mathrm{C}-\mathrm{C}=\mathrm{CH}-$ |  | $\mathrm{CH}_{3} \mathrm{r}-\mathrm{C}=\mathrm{C}=$ |
|  | = $\mathrm{C}-\mathrm{C}=\mathrm{C}$ - |  | $-\mathrm{CHr}-\mathrm{C}-\mathrm{C}=$ |

r: Ramification; c: Cycle.

Table 4. Different expressions of the $F(\theta)$ equation.

| Expression | Equation |
| :---: | :---: |
| $\theta=\mathrm{b}^{*}\left(\Sigma \mathrm{ni} . \Delta \theta \mathrm{i}+\Sigma \mathrm{n} j \Delta \theta_{\mathrm{j}}\right)$ | (1) |
| $\operatorname{Exp}(\theta / \mathrm{p})=\mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{\mathrm{i}}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (2) |
| $(1 / \theta){ }^{p}=b^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\sum n_{j} \Delta \theta_{j}\right)$ | (3) |
| $(\mathrm{M} / \theta)=\mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (4) |
| $(\mathrm{Tb} / \theta)=\mathrm{b}^{*}\left(\Sigma n_{i} . \Delta \theta \mathrm{i}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (5) |
| $\theta=a+b^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)$ | (6) |
| $\operatorname{Exp}(\theta / \mathrm{p})=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{ni}_{\mathrm{i}} . \Delta \theta_{\mathrm{i}}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (7) |
| $(1 / \theta)^{\mathrm{p}}=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{ni}_{i} \cdot \Delta \theta i+\Sigma \mathrm{n} j \Delta \theta_{\mathrm{j}}\right)$ | (8) |
| $(\mathrm{M} / \theta)=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{\mathrm{i}}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (9) |
| $(\mathrm{Tb} / \theta)=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{ni}^{2} . \Delta \theta_{\mathrm{i}}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)$ | (10) |
| $\theta=a^{+} \mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{\mathrm{i}}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)+\mathrm{c}^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)^{m}$ | (11) |
| $\operatorname{Exp}(\theta / p)=a^{+} b^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)+c\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{m}$ | (12) |
| $(1 / \theta)^{p}=a+b^{*}\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{\mathrm{j}}\right)+\mathrm{c}\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{\mathrm{j}}\right)^{m}$ | (13) |
| $(M / \theta)=a+b^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{\mathrm{j}}\right)+c\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{m}$ | (14) |
| $\left(\mathrm{T}_{\mathrm{b}} / \theta\right)=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)+\mathrm{c}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{\mathrm{j}} \Delta \theta_{\mathrm{j}}\right)^{m}$ | (15) |
| $\theta=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)+\mathrm{c}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)^{m}+\mathrm{d}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)^{n}$ | (16) |
| $\operatorname{Exp}(\theta / \mathrm{p})=\mathrm{a}+\mathrm{b}^{*}\left(\Sigma \mathrm{ni}_{i} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)+\mathrm{c}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)^{m}+\mathrm{d}\left(\Sigma \mathrm{n}_{\mathrm{i}} . \Delta \theta_{i}+\Sigma \mathrm{n}_{j} \Delta \theta_{\mathrm{j}}\right)^{n}$ | (17) |
| $(1 / \theta)^{p}=a^{+}+b^{*}\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)+c\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{m}+d\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{n}$ | (18) |
| $(M / \theta)=a^{+}+b^{*}\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)+c\left(\Sigma n_{i} \cdot \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{m}+d\left(\Sigma n_{i} . \Delta \theta_{i}+\Sigma n_{j} \Delta \theta_{j}\right)^{n}\left(T_{b} / \theta\right)=$ | (19) |
|  | (20) |

we retained for each parameter ( $A$ and $B$ ) the equations, having provided relatively the weakest variations compared to the bench-mark data for each family of hydrocarbon. We select Equation (11) for parameter "A" ( $\mathrm{A} A D \%=1.29 \%$ ) and Equation (19) ( $\mathrm{AAD} \mathrm{\%}=2.23 \%$ ) for the parameter " B ".

The values of the parameters $A$ and $B$ of the normal paraffin, isoparaffin, olefin, naphtene and aromatic are given in Tables 5 and 6.

## Validity of the correlation

Once this stage of determination of parameters $A$ and $B$ of the general equation $\left(\Delta H_{V}=A\left(1-\left(T / T_{C}\right)\right)^{B}\right)$ is completed, we carried out the calculation of the enthalpy of vaporization of pure hydrocarbons.
We tested the correlation for two temperatures (298,15 K and Teb ) so that to check the validity of our correlation whatever the selected temperature. Absolute
average deviations obtained by comparing the enthalpy of vaporization calculated by our correlation and that found in the data bank of "DIPPR" (1995) ( $\Delta \mathrm{H} \mathrm{v}$ of reference) are recorded in Table 7.
The variations recorded by our method compared to the reference are very weak. In the same way, we note that the variation in the temperature does not influence the validity of the proposed method.

## Comparison between the correlations established and other correlations of the literature

In this research, in order to further test the reliability of the suggested correlation, a study was undertaken by carrying out a comparison based on the AAD recorded by various methods available in the literature and the current correlation referring to the data bank for the five studied families of hydrocarbons.
We compared our correlation with correlation of Pitzer et al. (1955), Basarova and Svoboda (1995), and Vetere (1973). We also compared with the correlation of Ricardo (2005) using the correlation of Meyra et al. (2004), we note that the differences are greater than $20 \%$, so we changed the correlation Meyra et al. (2004) with adding the term k :

With: $k=3 Z_{c}$
Comparison of deviations recorded by the general equation established and correlations Pitzer et al. (1955),

Basarova and Svoboda (1995), Vetere (1973) and Ricardo (2005) are given in Table 8.

According to Table 8, the selected correlation gave weak variations compared to the reference at the normal boiling point and the other correlations for all the studied hydrocarbons families. In addition, The Hvb calculated from the established correlation remains close to that given by the reference.

## APPLICATION FOR SIMPLE MIXTURES

Twenty binary and ternary mixtures each, whose components belong either to the same family or to different families, were examined. Initially, the evaluation consists in the calculation of the different mixtures components properties; secondely, the mixture average property was determined; finally, the obtained results were compared with literature:
$\Delta H_{V m}=\frac{\sum_{v_{i}}^{\Delta H_{i} X_{i}}}{\sum^{X_{i}}}$
With: $\Delta H_{V m}$ : enthalpy of vaporization of the mixture in $\mathrm{kj} /$ mole; $\Delta \mathrm{H}_{V i}$ : enthalpy of vaporization of component «i» in the mixture ( $\mathrm{kj} / \mathrm{mole}$ ); $\mathrm{X}_{i}$ : molar fraction of component «i».

## Binary mixtures

The binary mixtures that we have studied are represented in the following Table 9. The results obtained during the calculation of the enthalpy of vaporization of the twenty (20) binary mixtures at $298,15 \mathrm{~K}$ are represented in the following Table 10.
By analyzing the results represented in the Table 10, we note that the absolute average deviations recorded by our correlation are weaker, compared to those obtained by the method of Pitzer and this for all the studied mixtures. Therefore, our correlation remains successfully applicable to binary mixtures.

## Ternary mixtures

We applied the same calculations to ternary mixtures whose compositions are shown in Table 11. The results obtained during the calculation of the enthalpy of vaporization of the 20 ternary mixtures at $298,15 \mathrm{~K}$ are represented in Table 12.
According to results from Table 12, compared to the correlation of Pitzer, the suggested correlation raised weaker variations for the majority of the studied mixtures. Therefore the established correlation for pure hydrocarbons applies correctly to ternary mixtures.

Table 5. Parameters of the selected correlations of group contribution with interactions for parameter A.

| n-parafffin : Equation 11 | Isoparaffin : Equation 11 |  |
| :---: | :---: | :---: |
| Parameter | Parameter |  |
| a -1602676.75 | a | 10158146.1 |
| b 14.1088334 | b | 16.4382549 |
| c 9375.83247 | c | 15261.1611 |
| $\mathrm{m} \quad 0.42073779$ | m | 0.46828699 |
| Structural groupings | Structural groupings |  |
| $-\mathrm{CH}_{3} \quad 306279.945$ | $-\mathrm{CH}_{3}$ | 164454.822 |
| - $\mathrm{CH}_{2}-\quad 161958.05$ | - $\mathrm{CH}_{2}-$ | 93320.7788 |
|  | $-\mathrm{CH}<$ | 430229.691 |
|  | $>\mathrm{C}<$ | 306635.302 |
| Principal groupings of interactions | Principal groupings of interactions |  |
| $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\quad 306279.945$ | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{2}-$ | -39332.5498 |
| $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\quad 2184463.261$ | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{3}$ | 7922.22325 |
| $-\mathrm{CH}_{3} \ldots .-\mathrm{CH}_{3} \quad 612558.89$ | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | 205730.41 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | -15433.7278 |
|  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}$ | 128223.231 |
|  | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}-$ | 96423.4456 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | 20643.9093 |
|  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{2}-$ | 8369.29125 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}_{2}-$ | -68031.6205 |
|  | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}-$ | 206113.841 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | 2819.22875 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}-$ | 43622.6622 |
|  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}-$ | 104740.089 |
|  | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{C}-$ | -143556.96 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}-$ | 83425.825 |
|  | $-\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}_{2}-$ | 54943.2509 |
|  | $-\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}-$ | 69440.8828 |

## APPLICATION OF THE METHOD ESTABLISHED TO OIL FRACTIONS

In this part of our work, we applied the correlations established to some oil fractions (light, averages and heavy) from an Algerian crude oil.

## Case of the light oil fractions

For this type of fractions, we apply the same step exactly as that adopted for simple mixtures, since the quantitative and qualitative composition of the fractions is known. We use the following relation:

$$
\begin{equation*}
\Delta H_{V / p}=\frac{\sum_{V i * X_{i}}^{\Delta H_{i}}}{\sum_{i}^{X}} \tag{8}
\end{equation*}
$$

With: $\Delta \mathrm{H}$ vfp : enthalpy of vaporization of oil fractions in $\mathrm{kj} / \mathrm{mole} ; \Delta \mathrm{H} \mathrm{v}_{i}$ : enthalpy of vaporization of component"i " in oil fraction (kj/mole); $\mathrm{X}_{\mathrm{i}}$ : molar fraction of component «i".

## Average and heavy oil fractions

We observed the rule of additivity and the assumption of the pseudo-components (hypothetical hydrocarbon) as follows:

While basing itself on the molar mass of the oil fraction

Since the oil fractions contain practically only three

Table 6. Parameters of the selected correlations of group contribution with interactions for parameter B.

| n-parafffin : Equation 19 |  | Isoparaffin : Equation 19 |  | Olefin : Equation 11 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Parameter | Value | Parameter | Value | Parameter | Value |
| a | 28.0053459 | a | 28.215093 | a | 4399888.55 |
| b | 82.8886734 | b | 85.516316 | b | 26079.5318 |
| c | -943.091941 | c | -337.291074 | c | 261221.607 |
| m | -3.20182293 | m | -2.27143952 | m | 0.1858332 |
| d | -943.091941 | d | -337.291074 |  |  |
| n | -3.20182293 | n | -2.27143952 |  |  |
| Structural grouping | Value | Structural grouping | Value | Structural grouping | Value |
| $-\mathrm{CH}_{3}$ | 0.66241163 | $-\mathrm{CH}_{3}$ | 0.89485725 | $-\mathrm{CH}_{3}$ | 261.969421 |
| - $\mathrm{CH}_{2}$ - | 0.7391905 | - $\mathrm{CH}_{2}-$ | 0.53841215 | - $\mathrm{CH}_{2}$ - | 256.308434 |
|  |  | $-\mathrm{CH}<$ | -0.4954034 | $-\mathrm{CH}<$ | 405.309306 |
|  |  | >C< | -0.9173492 | $>\mathrm{C}<$ | 220.10477 |
|  |  |  |  | $=\mathrm{CH}_{2}$ | 251.396698 |
|  |  |  |  | $=\mathrm{CH}-=\mathrm{C}<$ | 238.561754 |
| Principal grouping of interactions | Value | Principal grouping of interactions | Value | Principal grouping of interactions | Value |
| $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -0.33779364 | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{2}-$ | 0.01719311 | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -55.7753987 |
| $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -0.4523436 | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{3}$ | 0.03450571 | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -11.6329586 |
| $-\mathrm{CH}_{3} \ldots . \mathrm{CH}_{3}$ | 0.32456277 | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -0.27999073 | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}=$ | -51.643278 |
|  |  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}$ | 0.00632537 | $-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}_{2}$ | 119.895742 |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | -0.15324476 | $\mathrm{CH}_{3}-\mathrm{CH}=\mathrm{CH}-$ | 51.7924179 |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | -0.14058059 | $-\mathrm{CH}_{2}-\mathrm{CH}=\mathrm{CH}-$ | 51.7924179 |
|  |  | $\mathrm{CH}_{3}-\mathrm{C}_{2} \mathrm{CH}_{2}-$ | -0.0233563 | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}=$ | 6.05591567 |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}_{2}-$ | -0.04548205 | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}_{3}$ | -234.604872 |
|  |  | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}-$ | 0.07576622 | $\mathrm{CH}_{3}-\mathrm{C}=\mathrm{CH}-$ | -7.69474981 |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -0.25785315 | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{3}$ | 30.853715 |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}-$ | 0.03691472 | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{CH}=$ | 13.4378487 |
|  |  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}-$ | -0.05359021 | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}_{2}-$ | 11.4714888 |
|  |  | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{C}-$ | -0.1727451 | $\mathrm{CH}_{3}-\mathrm{C}=\mathrm{CH}_{2}-$ | 11.4135532 |
|  |  | $\mathrm{CH}_{3}-\mathrm{CH}-\mathrm{C}-$ | 0.16585181 | Terms | f position |
|  |  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}-$ | -0.22570371 | Cis | -68.4092800 |
|  |  |  |  | Trans | -67.6778359 |
|  |  | Naphtene | : Equation 11 | Aromatic | Equation11 |
|  |  | Parameter | Value | Parameter | Value |
|  |  |  | 16282193.3 |  | -15647428.6 |
|  |  | b | 22.1665989 | b | -4.81131743 |
|  |  | c | 12959.8011 | c | 68852.1317 |
|  |  | m | 0.5319444 | m | 0.50474669 |
|  |  | Structural grouping | Value | Structural grouping | Value |
|  |  | $-\mathrm{CH}_{3}$ | 44398.1163 | $-\mathrm{CH}_{3}$ | 53175.9389 |
|  |  | $-\mathrm{CH}_{2}-$ | 34389.882 | $-\mathrm{CH}_{2}-$ | 271456.811 |
|  |  | $-\mathrm{CH}<$ | 42917.0212 | $-\mathrm{CH}<$ | 302109.982 |
|  |  | $>\mathrm{C}<$ | 116771.968 | $>\mathrm{C}<$ | 477111.553 |
|  |  |  |  | $=\mathrm{CH}-$ | 43757.8544 |
|  |  |  |  | $=\mathrm{C}_{<}$ | 45563.544 |

Table 6. Contd.

| Principal grouping of interaction |  | Value | Principal grouping of | interaction | Value |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Cycle-Ramification | $-\mathrm{CH}_{2 \mathrm{r}}-\mathrm{CH}_{\mathrm{c}}-\mathrm{CH}_{2 \mathrm{c}}$ | 79670.3701 | Cycle - Ramification | $-\mathrm{CH}_{2} \mathrm{r}-\mathrm{C}-\mathrm{CH}=$ | 21889.4097 |
|  | $-\mathrm{CH}_{2 r-} \mathrm{CH}_{2 r-} \mathrm{CH}_{c}$ | 72271.4972 |  | $-\mathrm{CH}_{2 r}-\mathrm{C}=\mathrm{CH}-$ | -13316.1082 |
|  | $\mathrm{CH}_{3 r}-\mathrm{CH}_{c}-\mathrm{CH}_{2 \mathrm{c}}$ | 14607.2621 |  | $\mathrm{CH}_{3}-\mathrm{C}=\mathrm{CH}-$ | 88422,5709 |
|  | $\mathrm{CH}_{3 r-} \mathrm{CH}_{c}-\mathrm{CH}_{c}$ | 14381.1117 |  | $\mathrm{CH}_{3}-\mathrm{C}-\mathrm{CH}=$ | 12670,3175 |
|  |  |  |  | $\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}=$ | -110214,647 |
| Ramification | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | 72271.4972 | Ramification | $\mathrm{CH}_{3}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -110214.647 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | 131518.705 |  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}-$ | -16309.7454 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}_{2}$ | 89640,2866 | Cycle | $=\mathrm{CH}-\mathrm{CH}=\mathrm{CH}-$ | 82620,6895 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{CH}-$ | 35973,1679 |  | $=\mathrm{CH}-\mathrm{CH}=\mathrm{C}-$ | 26541,2225 |
|  | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}_{2}-$ | 61990,6156 |  | $-\mathrm{CH}=\mathrm{CH}-\mathrm{C}=$ | 173008,653 |
| Cycle | $-\mathrm{CH}_{2}-\mathrm{CH}-\mathrm{CH}-$ | 14381,1117 |  | $-\mathrm{CH}=\mathrm{C}-\mathrm{CH}=$ | 32624,6607 |
|  | - $\mathrm{CH}_{2}-\mathrm{CH}_{2}-\mathrm{C}-$ | 58385,4839 |  | $-\mathrm{C}=\mathrm{CH}-\mathrm{C}=$ | 136287,196 |
|  | - $\mathrm{CH}_{2}-\mathrm{C}-\mathrm{CH}_{2}-$ | 116770,968 |  | - $\mathrm{C}=\mathrm{C}-\mathrm{CH}=$ | 46436,9893 |
|  | $-\mathrm{CH}-\mathrm{CH}_{2}-\mathrm{CH}-$ | 3385,09777 |  | $=\mathrm{C}-\mathrm{C}=\mathrm{CH}-$ | 159008,901 |
|  |  |  |  | $=\mathrm{C}-\mathrm{C}=\mathrm{C}$ - | 168317,541 |
|  | Terms of position | Value |  |  |  |
|  | Cis | 159457.069 |  |  |  |
|  | Trans | 142117.832 |  |  |  |

Table 7. Average absolute deviations (AAD\%) recorded by the general equation for the calculation of the enthalpy of vaporization of pure hydrocarbons.

| Family | n-paraffin | Isoparaffin | Olefin | Naphtene | Aromatic | AAD\% |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{C}_{5}-\mathbf{C}_{\mathbf{1 9}}$ | $\mathbf{C}_{\mathbf{5}}-\mathbf{C}_{\mathbf{9}}$ | $\mathbf{C}_{\mathbf{5}}-\mathbf{C}_{\mathbf{2 0}}$ | $\mathbf{C}_{\mathbf{6}}-\mathbf{C}_{\mathbf{1 6}}$ | $\mathbf{C}_{\mathbf{6}}-\mathbf{C}_{\mathbf{2 4}}$ | - |
|  | 15 | 35 | 25 | 18 | 35 | 128 |
| Suggested correlation at 298,15 K | 0.8 | 0.95 | 0.83 | 0.46 | 1.06 | 0.87 |
| Suggested correlation at Teb | 0.69 | 0.86 | 0.4 | 0.52 | 1.28 | 0.82 |

Table 8. Comparison between the established correlation and correlations Pitzer et al. (1955), Basarova and Svoboda (1995), Vetere (1973) and Ricardo (2005) at the normal boiling point.

| Interval | Family | n-parafffin | Isoparaffin | Olefin | Naphtene | Aromatic | AAD \% |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathbf{C}_{5}-\mathbf{C}_{19}$ | $\mathbf{C}_{5}-\mathbf{C}_{9}$ | $\mathbf{C}_{5}-\mathbf{C}_{20}$ | $\mathbf{C}_{6}-\mathbf{C}_{16}$ | $\mathbf{C}_{6}-\mathbf{C}_{24}$ | - |
|  | 15 | 35 | 25 | 18 | 35 | 128 |  |
| Suggested correlation | 0.69 | 0.86 | 0.4 | 0.52 | 1.28 | 0.82 |  |
| Pitzer | 5.57 | 3.04 | 4.62 | 5.78 | 4.33 | 4.38 |  |
| Svoboda | 3.08 | 1.76 | 1.58 | 1.42 | 4.94 | 2.70 |  |
| Vetere | 2.44 | 1.23 | 0.90 | 1.72 | 1.94 | 1.57 |  |
|  |  |  |  |  |  |  |  |
| Nb pts | 15 | 27 | 25 | 16 | 35 | 119 |  |
| Ricardo et al. | $\mathrm{Z}_{\mathrm{c} 1}=0.292$ | 16.12 | 11.72 | 15.22 | 11.73 | 15.51 | 14.03 |
|  | $\mathrm{Z}_{\mathrm{c} 2}=0.27$ | 6.87 | 3.97 | 4.32 | 3.06 | 5.81 | 4.79 |
|  | $\mathrm{Z}_{\mathrm{c} 3}$ | 2.01 | 3.68 | 3.95 | 4.01 | 4.27 | 3.71 |

Table 9. List studied of binary mixtures.

| No. of the mixture | Components "1" | Components "2" |
| :---: | :--- | :--- |
| 1 | Hexane | Heptane |
| 2 | Benzene | Toluene |
| 3 | Hexane | Cycloheptane |
| 4 | Benzene | Cyclohéptane |
| 5 | Hexane | Benzene |
| 6 | Tridecane | Tetradecane |
| 7 | Pentadecane | Heptane |
| 8 | Heptane | Methylcyclohexane |
| 9 | Heptane | Ethylebenzene |
| 10 | Ethylbenzene | Hexane |
| 11 | Ethylbenzene | Nonane |
| 12 | methylcyclohexane | Heptane |
| 13 | Hexane | Nonane |
| 14 | Hexane | Heptane |
| 15 | Hexane | Heptane |
| 16 | Tetradecane | Hexane |
| 17 | Hexane | Decane |
| 18 | Benzene | Toluene |
| 19 | Benzene | Cycloheptane |
| 20 | Heptane | Methylcyclohexane |

families of hydrocarbons: aromatic paraffins and naphtenes, we compare our oil fractions to mixtures of these three families by using the following additivity rule:

$$
\begin{equation*}
\Delta H_{V F P}=\Delta H_{V p} * X_{P}+\Delta H_{V N} * X_{N}+\Delta H_{V A} * X_{A} \tag{9}
\end{equation*}
$$

With: $\mathrm{X}_{P}, \mathrm{X}_{N}$ and $\mathrm{X}_{A}$ : molar compositions of the fraction in: aromatic paraffins, naphtenes respectively; $\Delta \mathrm{H}_{V P}$, $\Delta \mathrm{H}_{V N}$ and $\Delta \mathrm{H}_{V A}$ : enthalpies of vaporizations of paraffin, naphtene and the aromatic (pure hydrocarbons) respectively having the same molar mass as the oil fraction.

The characteristics of the fractions used for the application of our correlation are gathered in Table 13. For the calculation of the composition of the oil fractions, we used the following Riazi-Daubert [12, 13] correlation:
For $\mathrm{MM}<200 \mathrm{~g} / \mathrm{mol}$ (light and average molar fractions)
$X_{P}=373,87-408,29 S p G r+1,4772 m$
$X_{N}=-150,27+210,152 S p G r-2,388 m$
$\mathrm{X}_{\mathrm{A}}=100-\left(\mathrm{X}_{\mathrm{P}}+\mathrm{X}_{\mathrm{N}}\right)$

For MM>200 g/mol (heavy fractions)
$X_{P}=198,42-27,772 R i-15,643 C H$
$X_{N}=59,77-76,174 R i+6,<8048 C H$
$\mathrm{X}_{\mathrm{A}}=100-\left(\mathrm{X}_{\mathrm{P}}+\mathrm{X}_{\mathrm{N}}\right)$

With: $m=M\left(n_{20}-1,4750\right) ; \mathrm{Ri}=\mathrm{n}_{20}-\mathrm{d}_{20} \underline{2}$

The results obtained are given in Table 14. For the light fraction, the mass molar is given by CPG. But for the average and the heavy fractions, it is calculated by the method of Riazi-Daubert; Xi : Composition of the various families obtained by the method of Riazi-Daubert (Riazi and Daubert. 1980, 1987),

## Light fractions

## First fraction

For the light fractions, we have the quantitative and qualitative composition obtained by CPG, as shows in Table 15.
We compared the results with the reference. They are recorded in Table 16. The results of the enthalpy of vaporization of the studied light fraction show that our equations are very close to the reference. This result was predictable becauce the enthalpy of vaporization of the fraction was calculated starting from a detailed composition and the correlations established in the case of pure hydrocarbons are very efficient.

## Average fractions

## Using the characterization based on the molar mass (MM)

For the second fraction, we suppose that the oil fraction can be comparable as normal paraffin at first, then as naphten and finally, as aromatique, which has the same molar mass as the cut that we have to treat. Compounds corresponding:
i. n-nonane for normal parrafin,
ii. n-propylcyclohexane for naphten, iii. n-propylbenzene for aromatic.

The values of each family of enthalpy of vaporization are calculated by the correlation suggested:
$\Delta H_{V P}=37,55 \mathrm{kj} / \mathrm{mol}$
$\Delta H_{V N}=35,44 \mathrm{kj} / \mathrm{mol}$
$\Delta H_{V A}=36,27 \mathrm{kj} / \mathrm{mol}$
Where the value of the enthalpy of vaporization of the oil fraction can be calculated as follows:
$\Delta H_{V F P}=\Delta H_{V p} * X_{P}+\Delta H_{V N} * X_{N}+\Delta H_{V A} * X_{A}$
With: $X_{P}=52.30 ; X_{N}=23.35 ; X_{A}=24.35$

Table 10. AAD (\%) recorded by the established correlation and other methods for the calculation of binary mixtures.

| Mixture | Composition \% molar |  | Reference value (KJ/mole) | Proposed correlation (KJ/mole) | Pitzer ( $\mathrm{KJ} / \mathrm{mole}$ ) | \% AAD |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Proposed |  |  | Pitzer |
| N ${ }^{\text {}}$ | \% mol ${ }_{1}$ | \% mol ${ }_{2}$ |  |  |  | correlation |  |
| 1 | 44 | 56 |  | 34.3904 | 34.6176 | 33.7644 | 0.66 | 1.82 |
| 2 | 45 | 55 | 36.0875 | 36.1545 | 35.4380 | 0.19 | 1.80 |
| 3 | 46 | 54 | 34.6072 | 34.6754 | 31.7310 | 0.20 | 8.31 |
| 4 | 55 | 45 | 35.3115 | 35.3015 | 32.6285 | 0.03 | 7.60 |
| 5 | 45 | 55 | 32.7555 | 32.8220 | 32.1110 | 0.20 | 1.97 |
| 6 | 48 | 52 | 68.2376 | 67.7520 | 63.1236 | 0.71 | 7.49 |
| 7 | 36 | 64 | 50.5980 | 50.4604 | 47.6508 | 0.27 | 5.82 |
| 8 | 44 | 56 | 36.0196 | 36.1876 | 35.1948 | 0.47 | 2.29 |
| 9 | 44 | 56 | 39.7604 | 40.0012 | 38.9356 | 0.61 | 2.07 |
| 10 | 62 | 38 | 38.1616 | 38.3526 | 37.4650 | 0.50 | 1.83 |
| 11 | 55 | 45 | 39.2140 | 39.3655 | 38.3540 | 0.39 | 2.19 |
| 12 | 56 | 44 | 33.7800 | 33.8952 | 33.1092 | 0.34 | 1.99 |
| 13 | 68 | 32 | 36.2216 | 36.4904 | 35.4972 | 0.74 | 2.00 |
| 14 | 17 | 83 | 35.7647 | 36.0243 | 35.0442 | 0.73 | 2.01 |
| 15 | 71 | 29 | 33.0161 | 33.2109 | 32.4846 | 0.59 | 1.61 |
| 16 | 38 | 62 | 46.3296 | 46.2388 | 43.8552 | 0.20 | 5.34 |
| 17 | 35 | 65 | 44.1045 | 44.5050 | 42.9075 | 0.91 | 2.71 |
| 18 | 17 | 83 | 37.2775 | 37.3837 | 36.7148 | 0.28 | 1.51 |
| 19 | 80 | 20 | 34.4440 | 34.4340 | 32.7960 | 0.03 | 4.78 |
| 20 | 65 | 35 | 36.2485 | 36.4585 | 35.4405 | 0.58 | 2.23 |
| \% AAD Average |  |  |  |  |  | 0.43 | 3.37 |

Table 11. Composition of ternary mixtures.

| No. of the mixture | Component "1" | Component "2" | Component "3" |
| :---: | :--- | :--- | :--- |
| 1 | Hexane | Heptane | Nonane |
| 2 | Hexane | Tetradecane | Tetradecane |
| 3 | Ethylcyclohexane | Benzene | Hexane |
| 4 | Cycloheptane | Toluene | Heptane |
| 5 | Heptane | Benzene | Toluene |
| 6 | Heptane | Ethylcyclohexane | Ethylcyclopentane |
| 7 | Tridecane | Tridecane | Ethylcyclohexane |
| 8 | Benzene | Toluene | Ethylebenzene |
| 9 | Benzene | Ethylbenzene | Tridecane |
| 10 | Benzene | Ethylbenzene | Ethylcyclopentane |
| 11 | Heptane | Tridecane | Hexane |
| 12 | Tridecane | Ethylcyclohexane | Benzene |
| 13 | Heptane | Decane | Ethylcyclopentane |
| 14 | Decane | Ethylcyclohexane | Ethylcyclopentane |
| 15 | Decane | Benzene | Toluene |
| 16 | Décane | Toluene | Ethylbenzene |
| 17 | Tridecane | Cycloheptane | Toluene |
| 18 | Tridecane | Ethylcyclohexane | Ethylbenzene |
| 19 | Benzene | Toluene | Hexane |
| 20 | Benzene | Toluene | Ethylcyclopentane |

Table 12. AAD (\%) recorded by the suggested method and other methods for the calculation of the ternary mixtures.

| Mixture | Composition |  |  | Reference value (kj/mole) | Proposed correlation (kj/mole) | Pitzer correlation (kj/mole) | \% AAD |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \% molar |  |  |  |  |  | Proposed | Pitzer |
| No. | \%mol 1 | \%mol 2 | \%mol3 |  |  |  | correlation |  |
| 1 | 27 | 32 | 41 | 39.17 | 39.50 | 38.25 | 0.86 | 2.35 |
| 2 | 17 | 43 | 40 | 61.85 | 61.48 | 57.58 | 0.61 | 6.91 |
| 3 | 34 | 34 | 32 | 35.37 | 35.37 | 33.96 | 0.00 | 3.97 |
| 4 | 27 | 39 | 34 | 37.32 | 37.47 | 35.52 | 0.38 | 4.83 |
| 5 | 31 | 31 | 38 | 36.26 | 36.39 | 35.57 | 0.37 | 1.90 |
| 6 | 32 | 30 | 38 | 37.90 | 37.99 | 36.38 | 0.25 | 4.01 |
| 7 | 37 | 43 | 20 | 62.50 | 62.08 | 57.89 | 0.66 | 7.37 |
| 8 | 20 | 36 | 44 | 39.01 | 39.14 | 38.28 | 0.35 | 1.86 |
| 9 | 15 | 60 | 25 | 46.85 | 46.86 | 45.12 | 0.01 | 3.69 |
| 10 | 19 | 62 | 19 | 39.59 | 39.74 | 38.70 | 0.38 | 2.24 |
| 11 | 26 | 52 | 22 | 50.69 | 50.56 | 48.13 | 0.27 | 5.06 |
| 12 | 48 | 24 | 28 | 50.79 | 50.53 | 47.77 | 0.52 | 5.95 |
| 13 | 15 | 49 | 36 | 43.69 | 44.03 | 42.40 | 0.79 | 2.94 |
| 14 | 44 | 27 | 29 | 44.03 | 44.26 | 42.23 | 0.52 | 4.09 |
| 15 | 40 | 28 | 32 | 41.96 | 42.21 | 40.92 | 0.60 | 2.47 |
| 16 | 37 | 29 | 34 | 44.20 | 44.50 | 43.16 | 0.69 | 2.34 |
| 17 | 24 | 58 | 18 | 44.23 | 44.13 | 40.21 | 0.22 | 9.08 |
| 18 | 19 | 16 | 65 | 46.45 | 46.47 | 44.59 | 0.05 | 3.99 |
| 19 | 29 | 28 | 43 | 33.99 | 34.09 | 33.42 | 0.30 | 1.66 |
| 20 | 23 | 23 | 54 | 36.40 | 36.49 | 35.53 | 0.25 | 2.40 |
| \% AAD Average |  |  |  |  |  |  | 0.40 | 3.96 |

Table 13. Characteristics of the studied oil fractions.

| Fraction |  | $\mathbf{T}_{\text {mav }}\left({ }^{\circ} \mathrm{C}\right)$ | SpGr | Kuop |
| :--- | :--- | :---: | :---: | :---: |
| Light | 1 Cut $\mathrm{C}_{5}-80^{\circ} \mathrm{C}$ | 52.67 | 0.6595 | 12.65 |
|  | 2 Cut $155-160^{\circ} \mathrm{C}$ | 157.5 | 0.7689 | 11.94 |
| Average | 3 Cut $195-200^{\circ} \mathrm{C}$ | 197.5 | 0.7926 | 11.94 |
|  | 4 Cut $250-260^{\circ} \mathrm{C}$ | 255.0 | 0.8211 | 11.98 |
|  |  |  |  |  |
|  | 5 Cut $270-280^{\circ} \mathrm{C}$ | 275.0 | 0.8352 | 11.92 |
| Heavy | 6 Cut $310-320^{\circ} \mathrm{C}$ | 315.0 | 0.8615 | 11.83 |
|  | 7 Cut $350-360^{\circ} \mathrm{C}$ | 355.0 | 0.8795 | 11.91 |

Kuop: Factor of characterization of Watson; SpGr: specific gravity; $\mathrm{T}_{\text {mav }}$ : average boiling point of the oil fraction.

Table 14. Characteristics of the oil fractions.

| Fraction |  | MM (g/mole) | $\% \mathbf{X P}_{\mathbf{P}}$ | $\% \mathbf{X}_{\mathbf{N}}$ | $\%_{\mathbf{X}}$ |
| :--- | :--- | :---: | :---: | :---: | :---: |
| Light | 1 Cut $\mathrm{C}_{5}-80^{\circ} \mathrm{C}$ | 69.39 | - | - | - |
|  | 2 Cut $155-160^{\circ} \mathrm{C}$ | 122 | 52.30 | 23.35 | 24.35 |
| Average | 3 Cut $195-200^{\circ} \mathrm{C}$ | 143 | 44.37 | 25.82 | 29.81 |
|  | 4 Cut $250-260^{\circ} \mathrm{C}$ | 186 | 35.81 | 26.83 | 37.36 |
|  |  |  |  |  |  |
| Heavy | 5 Cut $270-280^{\circ} \mathrm{C}$ | 201 | 68.57 | 23.05 | 8.38 |
|  | 6 Cut $310-320^{\circ} \mathrm{C}$ | 236 | 65.12 | 24.57 | 10.31 |
|  | 7 Cut $350-360^{\circ} \mathrm{C}$ | 280 | 64.01 | 25.14 | 10.85 |

MM: mass molar of the oil fractions.

Table 15. Composition of the fraction $\mathrm{C}_{5}-80^{\circ} \mathrm{C}$.

| No. | Name of constituent | \% Molar |
| :---: | :--- | :---: |
| 1 | Iso butane | 0.01 |
| 2 | n-butane | 0.16 |
| 3 | Iso pentane | 19.15 |
| 4 | n-pentane | 18.99 |
| 5 | 2,2-dimethyl butane | 2.30 |
| 6 | cyclopentane | 0.57 |
| 7 | 2,3-dimethyl butane | 3.18 |
| 8 | 2-methyl pentane | 14.65 |
| 9 | 3-methyl pentane | 8.37 |
| 10 | n-hexane | 16.99 |
| 11 | Methyl cyclo pentane | 3.17 |
| 12 | 2,2-dimethyl pentane | 1.16 |
| 13 | Benzene | 4.34 |
| 14 | 3,3-dimethyl pentane | 0.15 |
| 15 | cyclohexane | 2.70 |
| 16 | 2-methyl hexane | 1.50 |
| 17 | 2,3-dimethyl pentane | 0.58 |
| 18 | 3-methyl hexane | 1.07 |
| 19 | 1-cis-3-dimethyl cyclo pentane | 0.09 |
| 20 | 1-trans-3-dimethyl cyclo pentane | 0.12 |
| 21 | 3-ethyl pentane | 0.16 |
| 22 | n-heptane | 0.44 |
| 23 | Methyl cyclo hexane | 0.15 |
| Total |  | 100.00 |

Table 16. Results obtained for the fraction $\mathrm{N}^{\circ} 1$.

| $\mathbf{N}^{\circ} 1$ fraction | $\Delta \mathbf{H}$ v | \% AAD |
| :--- | :---: | :---: |
| Reference | 27.66 |  |
| Established correlation | 27.50 | 0.58 |
| Riazi-Daubert | 27.35 | 1.12 |

One obtains $\Delta H v_{F P}=36.75 \mathrm{kj} /$ mole (suggested correlation) and the enthalpy of vaporization of reference is $\Delta H v_{F P}=35.15 \mathrm{kj} / \mathrm{mole}$. We precede in the same way for the 3 other fractions and the results obtained are gathered in Table 17.

According to the results gathered in Table 18, we notice that our method gave weaker variations than those obtained by the correlation of Riazi-Daubert which presents itself relatively weak deviations compared to the reference.

## Heavy fractions

In the case of this type of fractions, the qualitative and quantitative composition is not known. We use the method of the pseudo-compound in order to calculate the
enthalpy of vaporization of these heavy fractions by the suggested correlation. We compare the results with the reference and the method of Riazi-Daubert.

Concerning the heavy fractions, we observe that the variations obtained by our correlation are relatively weakest compared to the reference. We can conclude that the correlaion established for pure hydrocarbons also apply properly to oil fractions (average and heavy).

## Conclusion

The present research was conducted to enrich the list by the existing empirical methods in the literature and aimed at approaching the thermodynamic properties, according to the temperature of pure hydrocarbons and their mixtures, in oil fractions.

These methods make it possible to avoid the recourse to experimental handling which is not always realizable.

The results obtained showed that the established correlation is reliable and presents weak variations compared to bank data for pure hydrocarbons. It is also applied to simple mixtures and oil fractions using the rule of additivity.

Compared with other correlation of the literature, our

Table 17. Calculated enthalpy of vaporization of the average fractions.

| Variable | FP2 | FP3 | FP4 |
| :--- | :---: | :---: | :---: |
| MM (g/mole) | 122 | 143 | 186 |
| n-parrafin | n-nonane | n-decane | n-tridecane |
| $\Delta H$ VP (Reference) | 37.32 | 39.60 | 46.53 |
| $\Delta H$ vP (Estimated) | 37.55 | 39.94 | 46.26 |
| Naphtene | n-propylcyclohexane | n-butylcyclohexane | n-heptylcyclohexane |
| $\Delta H$ vN (Reference) | 35.83 | 37.93 | 40.61 |
| $\Delta H$ vN (Estimated) | 35.44 | 38.26 | 41.18 |
| Aromatic | n-propylbenzene | n-pentylbenzene | octylbenzene |
| $\Delta H$ vA (Reference) | 38.07 | 42.47 | 47.78 |
| $\Delta H$ vA (Estimated) | 36.27 | 42.06 | 48.22 |
| $\%$ P | 52.30 | 44.37 | 35.81 |
| $\% ~ N$ | 23.35 | 25.82 | 26.83 |
| $\%$ A | 24.35 | 29.81 | 37.36 |
| $\Delta H$ VFP (Reference) | 37.15 | 40.02 | 45.41 |
| $\Delta H$ vFP (Estimated) | 36.75 | 40.14 | 45.63 |

Table 18. Variations recorded for the average fractions by our correlation and Riazi-Daubert correlation.

| FP | $\Delta H$ vFP (Reference) <br> $(\mathbf{K J} /$ mole $)$ | $\Delta H$ vFP (Estimated) <br> $(\mathbf{K J} /$ mole $)$ | Riazi-Daubert correlation <br> $(\mathbf{K J} /$ mole $)$ | Suggested <br> correlation | Riazi- <br> Daubert |
| :--- | :---: | :---: | :---: | :---: | :---: |
| FP 2 | 37.15 | 36.75 | 37.65 | 1.08 | 1.35 |
| FP 3 | 40.02 | 40.14 | 41.68 | 0.30 | 4.15 |
| FP 4 | 45.41 | 45.63 | 47.55 | 0.48 | 4.71 |

Table 19. Calculated enthalpy of vaporization of the heavy fractions.

| Variable | FP5 | FP6 | FP7 |
| :--- | :---: | :---: | :---: |
| MM (g/mole) | 201 | 236 | 280 |
| n-Parrafin | n-Tetradecane | n-Heptadecane | n-Eicosane |
| $\Delta H$ vP (Reference) | 47.88 | 53.53 | 56.45 |
| $\Delta H$ vP (Estimated) | 48.10 | 53.09 | 57.38 |
| Naphtene |  |  |  |
| $\Delta H$ vN (Reference) | n-Nonylcyclopentane | Dodecylcyclopentane | Tetradecyclohexane |
| $\Delta H$ vN (Estimated) | 51.75 | 58.13 | 64.89 |
|  | 50.82 | 58.85 | 65.40 |
| Aromatic |  |  |  |
| $\Delta H$ va (Reference) | n-Nonylbenzene | Undecylbenzene | Tetradecylbenzene |
| $\Delta H$ vA (Estimated) | 45.16 | 54.21 | 59.28 |
| $\%$ P | 49.91 | 53.32 | 58.11 |
| \% N | 68.57 | 65.12 | 64.01 |
| \% A | 23.05 | 24.57 | 25.14 |
| $\Delta H$ vFP (Reference) | 8.38 | 10.31 | 10.87 |
| $\Delta H$ vFP (Estimated) | 48.54 | 54.73 | 58.89 |

Table 20. Variations recorded for the heavy fractions by our correlation and Riazi-Daubert correlation.

| FP | $\Delta H$ vfp (Reference) (KJ/mole) | $\Delta H_{\text {vFP }}$ (Estimated) (KJ/mole) | Method of Riazi-Daubert (KJ/mole) | \% AAD |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Suggested correlation | Riazi-Daubert |
| FP 5 | 48.54 | 48.88 | 49.62 | 0.70 | 2.22 |
| FP 6 | 54.73 | 54.53 | 53.78 | 0.37 | 1.74 |
| FP 7 | 58.89 | 59.49 | 57.99 | 1.02 | 1.53 |

## Notations

AAD, Average absolute deviation (\%); a, b, c, d, m, n and p , parameters of the equations of group contribution with interactions; $A$ and $B$, parameters of the equation of the enthalpy of vaporization; $n_{i}$, number of structural groups of type " i "; $\mathrm{n}_{\mathrm{j}}$, number of principal groups of interactions of the type "j"; $\Delta \mathrm{H}_{\mathrm{v}}$, enthalpy of vaporization; $\Delta \mathrm{H} v M$, enthalpy of vaporization of the mixture; $\Delta \mathrm{H} V f p$, enthalpy of vaporization of the oil fraction; $\Delta H v i$, enthalpy of vaporization of component i ; Xi , molar fraction of component i; Tc, critical temperature; Teb, boiling point; R, constant of perfect gases; Kuop, factor of characterization of Watson; $\mathrm{d}_{20}$, density with $20^{\circ} \mathrm{C} ; \mathrm{n}_{20}$, index of refraction at $20^{\circ} \mathrm{C}$; MM, molar mass; SpGr , specific-gravity; DIPPR, Design Institute for Physical Property data.

## Greek letters

$\Theta$, Parameters of the studied property; $\Delta \theta \mathrm{i}$, contribution of the structural group of type "i"; $\Delta \theta \mathrm{j}$, contribution of the principal group of interaction of the type "j".

## Indices

A, Aromatic; N, naphtenic; P, paraffin; FP, oil fraction; eb, boiling; C, critical; I, a component in the mixture; mav, mean average; mol, molar.

## REFERENCES

Basarova P, Svoboda V (1995). Prediction of the Enthalpy of Vaporization by the Group Contribution Method", Fluid Phase Equilib., 105: 27-47.

Chen NH (1965). Generalized correlation for latent heat of vaporization. J. Chem. Eng. Data., 10: 207-210

Constantinou L, Gani R (1994). ). A New Group Contribution Method for the Estimation of Properties of Pure Compounds. Aiche J., 40(10): 1697-1710.
DIPPR (1995). Design Institute of Chemical Engineers. Complication of Pure Properties Compound dated.
Guggenheim EA (1945). The principle of corresponding states, J. Chem. Phys., 13: 253-261.
Kay WB (1936). Density of hydrocarbon gases and vapors at high temperature and pressures. Ind. Eng. Chem., 28: 1014-1019.
Li P, Liang YH, Ma PS, Zhu C (1997). "Estimations of enthalpies of vaporization of pure compounds at different temperatures by a corresponding-states group-contribution method." Fluid Phase Equilibria, 137: 63-74.

Meyra AG, Kuz VA, Zarragoicoechea GJ (2004). Universal behavior of the enthalpy of vaporization: An empirical equation. Fluid Phase Equilibria, 218: 205-207.
Pitzer KS,. Lippmann DZ, Curl RF, Huggins CM, Petersen DE (1955). The volumetric and thermodynamic properties of fluids. Theoretical bassis and virial coefficients. J. Am. Chem. Soc., 77(3433).
Reid RC, Prausnitz JM, Poling BE (2005). The Properties of Gases and Liquids. $4^{\text {th }}$ ed., McGraw-Hill, USA. pp. 205
Riazi MR, Daubert TE (1980). "Simplify Property Predictions." Hydrocarbon Process, 115-16.
Riazi MR, Daubert TE (1987). "Characterization Parameters for Petroleum Fractions." Ind. Eng. Chem. Res., 26(4): 755-759.
Ricardo AM, Ricardo MA (2005). Behavior of the empirical methods for prediction of vaporization enthalpy. (Eds.) Edio J. Alves, Moilton R. Franco Jr. Fluid Phase Equilibria, 236: 256-260
Skander N, Souahi F, Chitour CE (1999). Application of group contribution methods to estimate the acentric factor of hydrocarbon mixtures and petroleum fractions. Review of Entropy Publishing, pp 216.

Svoboda V, Dockalova P (1990). Extension of the group contribution method for the calculation of the heat of vaporization. Fluid Phase Equilibria, 54: 293-299.
Vetere A (1973). New Generalized Correlations for Enthalpy of Vaporization of Pure Compounds. Laboratori Ricerche Chimica Industriale, SNAM PROGETTI, San Donato Milanese.
Watson KM (1943). DIPPR Equation of heat vaporization. Cryogenics, 13: 470-482.


[^0]:    *Corresponding author. E-mail: rebasouardia@yahoo.fr.

